An EPQ Model of Exponential Deterioration With Fuzzy Demand and Production With Shortages

S. Sarkar* & T. Chakrabarti

Sanchita Sarkar, M.Sc., Technology, University of Calcutta,
Tripti Chakrabarti, Head and Professor Calcutta University, triptichakrabarti@gmail.com

KEYWORDS

Economic production quantity, Fuzzy demand, Fuzzy production inventory model, Fuzzy total cost

ABSTRACT

In the fundamental production inventory model, in order to solve the economic production quantity (EPQ) we always fix both the demand quantity and the production quantity per day. But, in the real situation, both of them probably will have little disturbances every day. Therefore, we should fuzzify both of them to solve the economic production quantity (q*) per cycle. Using α-cut for defuzzification the total variable cost per unit time is derived. Therefore the problem is reduced to crisp annual costs. The multi-objective model is solved by Global Criteria Method with the help of GRG (Generalized Reduced Gradient) Technique. In this model shortages are permitted and fully backordered. The purpose of this paper is to investigate a computing schema for the EPQ in the fuzzy sense. We find that, after defuzzification, the total cost in fuzzy model is less than in the crisp model. So it permits better use of the EPQ model in the fuzzy sense arising with little disturbances in the production, and demand.

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1. Introduction

For solving the EPQ for each cycle, we always fix both the demand quantity and production quantity per day in the crisp model. But, in the real situation, both of them probably will have some little disturbances per day. In recent years, many researchers have studied inventory models for deteriorating items such as electronic components, food items, drugs and fashion goods. Deterioration is defined as decay, change or spoilage that prevent the items from being used for its original purpose.

There are many items in which appreciable deterioration can take place during the normal storage period of the units and consequently this loss must be taken into account when analyzing the model. Therefore, many authors have considered Economic order quantity models for deteriorating items.

Acting as the driving force of the whole inventory system, demand is a key factor that should be taken into consideration in an inventory study. There are mainly two categories of demands in the present studies, one is deterministic demand and the other is stochastic demand. Some noteworthy work on deterministic demand are: Chung and Lin [1,2] have considered constant demand, Giri and Chakrabarti[3] and Teng and Chang[4] have considered time-dependent demand where as Giri and Chaudhuri[6], Bhattacharya[7] and Wu.et.al[8] have worked on inventory level-dependent demand and Wee and Law[9] have considered price-dependent demand.

Among them, ramp type demand is a special type of time-dependent demand. Hill[10] was the first to introduce the ramp type demand to the inventory study. Then Mandal and Pal[11] introduced the ramp type demand to the inventory study of the deteriorating items. Deng.et.al[12] and Shah and Jaiswal[13] have extensively studied this type of demand. Stochastic demand includes two types of demands: the first type characterized by a known demand distribution and the
second type characterized by arbitrary demand distribution i.e. demand is fuzzy in nature.
In the classical inventory model depletion of inventory is caused by a constant demand rate alone. But
subsequently, it was noticed that depletion of inventory may take place due to deterioration also. In the early
stage of the study, most of the deteriorating rates in the models are constant, Padmanabhan and Vrath [14],
and Bhunia and Maiti [15] worked on constant deterioration rate.
In recent research, more and more studies have begun to consider the relationship between time and
deteriorating rate. Wee [18], and Mahapatra [19], considered deterioration rate as linear increasing
function of time. Chakrabarty et al. [20] have considered three-parameter Weibull distribution. In this
connection, studies of many researchers like Ghare and Schrader [21], Goyel et al. [22] are very important.
Misra [23] developed a two parameter Weibull distribution deterioration for an inventory model. This
investigation was followed by Shah and Jaiswal [24], Aggarwal [25], Dave and Patel [26], Datta and Pal
[27], Jalan, Giri and Chaudhuri [28], Dixit and Shah [29], Giri and Goyel [30], Shah and Shah [31] etc.
The assumption of constant demand rate is not always appropriate for many inventory items. The works done
by Donaldson [32], Silver [33], Ritchie [34], Pal and Mandal [35] are to be mentioned regarding time
dependent demand rates.
In the present paper, efforts have been made to analyze an EPQ model that deteriorates exponentially assuming
demand rate to be exponential. Here production is demand dependent. To make the model more realistic
demand has been fuzzified. This paper investigates a new model which has been fuzzified. The works done
by Donaldson [32], Silver [33], Ritchie [34], Pal and Mandal [35] are very important.

2. Assumptions and Notations.

2.1. Notations:

a) Replenishment rate is finite and it is demand dependent.
b) Lead time is zero.
c) T the cycle time.
d) I(t) inventory level at time t.
e) C_i is the holding cost per unit time.
f) C_s is the shortage cost per unit time.
g) C_u is the unit purchase cost.
h) C_f is the fixed ordering cost of inventory.
i) θ deterioration rate of finished items.

2.2. Assumptions:

a) The demand is taken as exponential, R(t) = ae^{bt}.
b) Rate of production varies with demand i.e. K = βR(t) where β is constant.
c) Replenishment is instantaneous.
d) Lead-time (i.e. the length between making of a decision to replenish an item and its actual addition to stock) is assumed to be zero. The assumption is made so that the period of shortage is not affected.
e) The rate of deterioration at any time t>0 is dependent on time.
f) Shortages are allowed and are fully backlogged.


Here we assume production starts at t=0 at the rate K and the stock attains a level Q at t=1. The
production stops at t=1 and the inventory gradually depletes to zero at t=2 mainly to meet the demands
and partly for deterioration. Now shortages occur and accumulate to the level S at t=3. The production
starts again at a rate K at t=3 and the backlog is cleared at time t=T when the stock is again zero. The cycle
then repeats itself after time T.
The model is represented by the following diagram:

![Fig. 1. The model is represented by the following diagram](image)

Let I(t) be the inventory level at any time t(0 ≤ t ≤ T) and demand rate R(t) is assumed to be deterministic
and is increasing exponentially with time.

Further let R(t) = a e^{bt}, 0 ≤ b < 1, a > 0.
The differential equations describing instantaneous state of I(t) in the interval [0, T] are:

\[
\frac{dI(t)}{dt} + θI(t) = ae^{bt} \quad (1)
\]

\[
\frac{dI(t)}{dt} + θI(t) = -ae^{bt} \quad (2)
\]

\[
\frac{dI(t)}{dt} = -ae^{bt} \quad t_2 ≤ t ≤ t_3 \quad (3)
\]

\[
\frac{dI(t)}{dt} = -(β - 1)ae^{bt} \quad t_3 ≤ t ≤ T \quad (4)
\]
with the initial conditions \( I(t_0) = 0 \), \( I(t_1) = Q \)

Now solving the above differential equations we get:

\[
I(t) = a(\beta - 1)(t + \frac{b_1 t^2}{2} + \frac{b_2 (t_1^2 - t^2)}{3} + \frac{b_3 t^3}{3} + \frac{b_4 t^4}{4}) \quad 0 \leq t \leq t_1
\]

\[
I(t) = Q + a(t_1 - t) + \frac{b_1 t^2}{2} + \frac{b_2 (t_1^2 - t^2)}{3} + \frac{b_3 t^3}{3} + \frac{b_4 t^4}{4} \quad t_1 \leq t \leq t_2
\]

\[
I(t) = a(\beta - 1)(e - e^-) + \frac{b_2}{3} (t_2 - t^2) \quad t_2 \leq t \leq t_3
\]

\[
I(t) = \frac{a(\beta - 1)(t - t_3)^2}{b} \quad t_3 \leq t \leq T
\]

Holding Cost (H.C) over the period \([0, T]\)

\[
\text{Total average Cost} = C \int_0^T \text{Cost dt}
\]

\[\text{Set up Cost} = C_4\]

\[\text{Shortage Cost (S.C)}\] over the period \([0, T]\)

\[
\text{Deteriorating Cost} = C_3 \int_0^T \left( P - D \right) dt - C_3 \int_0^T D dt
\]

\[
\text{Set up Cost} = C_4
\]
Using the initial conditions the total average cost becomes function of \( t_1 \) and \( T \). Hence we find the global optimal solution of total average cost by using LINGO 12. And the minimum cost in the deterministic model is compared with the minimum cost in fuzzy model.

4. Fuzzy Model and Solution Procedure

The instantaneous states of the inventory level \( I(t) \) at time \( t(0 \leq t \leq T) \) can be described by the following equations:

\[
\frac{dI(t)}{dt} + \theta I(t) = ae^{t} (\beta - 1) \quad 0 \leq t \leq t_1
\]

\[
\frac{dI(t)}{dt} + \theta I(t) = -ae^{t} \quad t_1 \leq t \leq t_2
\]

\[
\frac{dI(t)}{dt} = -ae^{t} \quad t_2 \leq t \leq t_3
\]

\[
\frac{dI(t)}{dt} = (\beta - 1)ae^{t} \quad t_3 \leq t \leq T
\]

With the initial conditions \( I(t_0)=0, I(t_1)=Q, I(t_2)=0, I(T)=S \).

The differential equations (16) to (19) are fuzzy differential equations. To solve this differential equation at first we take the \( \alpha \)-cut then the differential equations reduces to

\[
\frac{dI^\alpha(t)}{dt} + \theta I^\alpha(t) = a^\alpha e^{bt} (\beta - 1) \quad 0 \leq t \leq t_1
\]

\[
\frac{dI^\alpha(t)}{dt} + \theta I^\alpha(t) = a^\alpha e^{bt} \quad t_1 \leq t \leq t_2
\]

\[
\frac{dI^\alpha(t)}{dt} = -a^\alpha e^{bt} \quad t_2 \leq t \leq t_3
\]

\[
\frac{dI^\alpha(t)}{dt} = (\beta - 1)a^\alpha e^{bt} \quad t_3 \leq t \leq T
\]

Now solving the above differential equations we get

\[
I_1^+(t) = \{a_3 - a(a_3 - a_2)\}/(\beta - 1)
\]

\[
I_1^-(t) = a_1 + a(a_2 - a_1)/(\beta - 1)
\]

\[
I_2^+(t) = Q + \{a_3 - a(a_3 - a_2)\}/(t_1 - t) + b(t_1^2 - t^2) + b^2(t_1^3 - t^3) + b^2\theta(t^5 - t_1^5)
\]

\[
I_2^-(t) = Q + \{a_3 - a(a_3 - a_2)\}/(t_1 - t) + b(t_1^2 - t^2) + b^2(t_1^3 - t^3) + b^2\theta(t^5 - t_1^5)
\]

\[
I_3^+(t) = \{a_3 - a(a_3 - a_2)\}/b \quad t_2 \leq t \leq t_3
\]

\[
I_3^-(t) = \{a_3 - a(a_3 - a_2)\}/b \quad t_2 \leq t \leq t_3
\]

\[
I_4^+(t) = (\beta - 1)a_1 + a(a_2 - a_1)/(e^{bt_3} - e^{bt}) \quad t_3 \leq t \leq T
\]

\[
I_4^-(t) = (\beta - 1)a_1 + a(a_2 - a_1)/(e^{bt_3} - e^{bt}) \quad t_3 \leq t \leq T
\]

\[
I_5^+(t) = (\beta - 1)a_1 + a(a_2 - a_1)/(e^{bt_3} - e^{bt}) \quad t_3 \leq t \leq T
\]

\[
I_5^-(t) = (\beta - 1)a_1 + a(a_2 - a_1)/(e^{bt_3} - e^{bt}) \quad t_3 \leq t \leq T
\]
\[
I'(t) = \frac{(\beta - 1)[a_3 - a(a_3 - a_2)]}{b}(e^{-bt} - e^{-bt})
\]

(35)

\[+S \leq t \leq T \]

Therefore the upper \( \alpha \) - cut of fuzzy stockholding cost \((HC^+)\)

\[
= C_1 \left\{ \int_0^t I'_{I_1}(t)dt + \int_{t_1}^{t_2} I'_{I_2}(t)dt \right\}
\]

\[= \{a_3 - a(a_3 - a_2)\}C_1(\beta - 1)
\]

\[
= \frac{t_1}{2} + \frac{b^2}{6} + \frac{b^2 t_1^4}{12} + \frac{\theta r_1^4}{12} + \frac{\theta r_1^6 b^2}{36}
\]

\[+ C_1\{Q(t_2 - t_1) + a(t_1 t_2 - \frac{t_2}{2})\}
\]

(36)

And the lower \( \alpha \)-cut of fuzzy stockholding cost \((HC^-)\) = \(C_1\left\{ \int_0^t I'_{I_1}(t)dt \right\}

\[
= \frac{t_1}{2} + \frac{b^2}{6} + \frac{b^2 t_1^4}{12} + \frac{\theta r_1^4}{12} + \frac{\theta r_1^6 b^2}{36}
\]

\[+ C_1\{Q(t_2 - t_1) + a(t_1 t_2 - \frac{t_2}{2})\}
\]

(37)

As demand is fuzzy in nature shortage cost is also fuzzy in nature.

\[= C_2 \left\{ \int_0^t I'_{I_1}(t)dt + \int_{t_1}^{t_2} I'_{I_2}(t)dt \right\}
\]

\[= \frac{t_1}{2} + \frac{a_3 + a(a_3 - a_2)}{b}(e^{-bt} - e^{-bt})
\]

\[+ C_2[\{a_3 + a(a_3 - a_2)\}]b
\]

\[\frac{b}{b^2}
\]

\[\int_{t_1}^{t_2} I'_{I_2}(t)dt
\]

\[\frac{\{\beta - 1\}[a_3 + a(a_3 - a_2)]}{b}(e^{-bt} - e^{-bt})
\]

\[+ C_2 S(T - t_2)
\]

(38)

Also the lower \( \alpha \)-cut of shortage cost \((SC^-)\) = \(C_2\left\{ \int_0^t I'_{I_1}(t)dt \right\}

\[\frac{t_1}{2} + \frac{a_3 + a(a_3 - a_2)}{b}(e^{-bt} - e^{-bt})
\]

\[+ C_2 S(T - t_2)
\]

(39)

Since demand is fuzzy in nature and production is dependent in demand so production is also fuzzy. So deterioration cost is also fuzzy in nature.

Deteriorating Cost = \(C_3\left\{ (P - D)dt + C_3 \int_{t_1}^{t_2} Ddt \right\}

\[= \frac{t_1}{2} + \frac{a(a_3 - a_2)}{b}(e^{-bt} - e^{-bt})
\]

\[+ C_3 S(T - t_2)
\]

(40)

Upper \( \alpha \)-cut of deterioration Cost \((DC^+)\)
Lower \( \alpha \)-cut of deterioration Cost \((DC^-)\)  
\[
DC^- = C_3(\beta - 1)\left\{ \frac{a_1 + a(a_3 - a_j)}{b \left( e - 1 \right) \left( 1 - \alpha \right)} \right\} + a_2 \frac{b^{t_1} - 1}{b} + \frac{a_3 \left( e - 1 \right) - e}{b} 
\]
(41)

Annual ordering Cost \(= C_4 \)

Therefore total variable cost per unit time is a fuzzy quantity and is defined by

\[
TVC^- = \inf \{ x \in R : \beta_{TVC}(x) \geq \alpha \}, \\
TVC^+ = \sup \{ x \in R : \beta_{TVC}(x) \geq \alpha \}, \\
TVC^+ = \{ a_3 - a(a_3 - a_j) \}/C_1(\beta - 1) \\
\left\{ \frac{1}{2} \left[ \frac{b^3 t_1}{3} + \frac{b^3 t_2}{3} \right] + \frac{b^2 t_1 t_2}{6} \right\} - \frac{bt_1 t_2}{2} - \frac{bt_1 t_2}{2} \\
+ C_3(\beta - 1)\left\{ a_1 + a(a_3 - a_j) \right\} \left( e - 1 \right) \left( 1 - \alpha \right)
\]
(43)

\[
TVC^+ = \sup \{ x \in R : \beta_{TVC}(x) \geq \alpha \}, \\
TVC^- = \inf \{ x \in R : \beta_{TVC}(x) \geq \alpha \}, \\
TVC^+ = \{ a_3 - a(a_3 - a_j) \}/C_1(\beta - 1) \\
\left\{ \frac{1}{2} \left[ \frac{b^3 t_1}{3} + \frac{b^3 t_2}{3} \right] + \frac{b^2 t_1 t_2}{6} \right\} - \frac{bt_1 t_2}{2} - \frac{bt_1 t_2}{2} \\
+ C_3(\beta - 1)\left\{ a_1 + a(a_3 - a_j) \right\} \left( e - 1 \right) \left( 1 - \alpha \right)
\]
(44)

\[
\frac{a_2 (e - 1)}{b} + C_3 \left\{ a_1 + a(a_3 - a_j) \right\} \left( e - 1 \right) \left( 1 - \alpha \right)
\]

The upper \( \alpha \)-cut of total variable cost per unit time is

\[
TVC^+ = \{ a_1 + a(a_3 - a_j) \}/C_1(\beta - 1) \\
\left\{ \frac{1}{2} \left[ \frac{b^3 t_1}{3} + \frac{b^3 t_2}{3} \right] + \frac{b^2 t_1 t_2}{6} \right\} - \frac{bt_1 t_2}{2} - \frac{bt_1 t_2}{2} \\
+ C_3(\beta - 1)\left\{ a_1 + a(a_3 - a_j) \right\} \left( e - 1 \right) \left( 1 - \alpha \right)
\]
(45)

\[
\frac{a_2 (e - 1)}{b} + C_3 \left\{ a_1 + a(a_3 - a_j) \right\} \left( e - 1 \right) \left( 1 - \alpha \right)
\]

Subject to \( 0 \leq \alpha \leq 1 \)

A convex function is a continuous function whose value at the midpoint of every interval in its domain does not exceed the arithmetic mean of its values at the ends of the interval.

More generally , a function \( f(x) \) is convex on an interval \([a, b]\) if for any two points \( x_1 \) and \( x_2 \) in \([a, b]\) and any \( \lambda \) where \( 0 < \lambda < 1 \), \( f(\lambda x_1 + (1- \lambda) x_2) \leq \lambda f(x_1) + (1- \lambda) f(x_2) \).

If \( f(x) \) has a second derivative in \([a, b]\), then a necessary and sufficient condition for it to be convex on that interval is that the second derivative \( f''(x) \geq 0 \) for all \( x \) in \([a, b]\).

Here \( TVC^- \) and \( TVC^+ \) are convex function as second order derivative of both \( TVC^- \) and \( TVC^+ \) positive. Hence the local minimum of the above functions also becomes the global minimum.

Therefore the problem is a multiobjective optimization problem.To convert it as a single objective
optimization problem we use global criteria (GC) method.
Then the above problem reduces to
\[
\text{Minimize} \quad GC \quad \text{(48)}
\]
Subject to \(0 \leq \alpha \leq 1\)

5. Global Criteria Method
The model presented by (47) is a multi-objective model which is solved by Global Criteria (GC) Method with the help of Generalized Reduced Gradient Technique.
The Multi-Objective Non-linear Integer Programming (MONLIP) problems are solved by Global Criteria Method converting it to a single objective optimization problem. The solution procedure is as follows:

Step-1: Solve the multi-objective programming problem (34) as a single objective problem using only one objective at a time ignoring other.

Step-2: From the results of Step-1, determine the ideal objective vector, say \((TVC^{\min}, TVC^{\min})\) and the corresponding values of \((TVC^{\max}, TVC^{\max})\). Here, the ideal objective vector is used as a reference point. The problem is then to solve the following auxiliary problem:

\[
\text{Min}(GC) = \text{Minimize} \left[ \frac{TVC^+ - TVC^{\min}}{TVC^{\max} - TVC^{\min}} \right] \quad Q \quad \text{ } \left( \frac{TVC^+ - TVC^{\max}}{TVC^+ - TVC^{\min}} \right) \quad \text{where } L \leq Q \leq Y. \text{ This method is also sometimes called Compromise Programming.}
\]

6. Numerical Example
We now consider a numerical example showing the utility of the model from practical point of view. According to the developed solution procedure of the proposed inventory system, the optimal solution has been obtained with the help of well known generalized reduced gradient method (GRG). To illustrate the developed model, an example with the following data has been considered:

Deterministic Model:
\(C_1 = \$8\) per unit, \(C_2 = \$9\) per unit, \(C_3 = \$5\) per unit, \(C_4 = \$100\) per order, \(b = 0.5\), \(\beta = 0.25\), \(\beta = 1\), \(q = 50\), \(t_0 = 0.001\), \(t_0 = 0.06\) T = 10hrs.
Substituting above parameters, Global Criteria (GC) is obtained as \(GC = 0.0044436\)
The compromise solutions are \(TVC^+ = \$ 25.52763\), \(TVC^- = \$ 25.90769\)

Now we will test the sensitivity of the optimal solution with respect to demand parameters \(a\) and \(b\) and production parameter \(\beta\) in deterministic model.

<p>| Tab. 1. Optimal cost for deterministic model |</p>
<table>
<thead>
<tr>
<th>Parameter (a)</th>
<th>% change</th>
<th>Value of the Parameter</th>
<th>Optimal cost for deterministic Model</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.9</td>
<td>+25%</td>
<td>2.375</td>
<td>142.643</td>
</tr>
<tr>
<td>1.9</td>
<td>-25%</td>
<td>1.425</td>
<td>170.405</td>
</tr>
<tr>
<td>1.9</td>
<td>50%</td>
<td>2.85</td>
<td>131.621</td>
</tr>
<tr>
<td>1.9</td>
<td>-50%</td>
<td>.95</td>
<td>183.056</td>
</tr>
</tbody>
</table>

<p>| Tab. 2. Optimal cost for deterministic model |</p>
<table>
<thead>
<tr>
<th>Parameter (b)</th>
<th>% change</th>
<th>Value of the Parameter</th>
<th>Optimal cost for deterministic model</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.5</td>
<td>+25%</td>
<td>0.625</td>
<td>135.57</td>
</tr>
<tr>
<td>0.5</td>
<td>-25%</td>
<td>0.375</td>
<td>183.96</td>
</tr>
<tr>
<td>0.5</td>
<td>50%</td>
<td>0.75</td>
<td>120.416</td>
</tr>
<tr>
<td>0.5</td>
<td>-50%</td>
<td>0.25</td>
<td>228.373</td>
</tr>
</tbody>
</table>

<p>| Tab. 3. Optimal cost for deterministic model |</p>
<table>
<thead>
<tr>
<th>Parameter (\beta)</th>
<th>% change</th>
<th>Value of the Parameter</th>
<th>Optimal cost for deterministic model</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>+25%</td>
<td>1.25</td>
<td>171.481</td>
</tr>
<tr>
<td>1</td>
<td>-25%</td>
<td>0.75</td>
<td>136.499</td>
</tr>
<tr>
<td>1</td>
<td>50%</td>
<td>1.5</td>
<td>183.224</td>
</tr>
<tr>
<td>1</td>
<td>-50%</td>
<td>0.5</td>
<td>263.124</td>
</tr>
</tbody>
</table>

Next we will test the sensitivity of the optimal solution with respect to demand parameter \(b\) and production parameter \(\beta\) in fuzzy model.

<p>| Tab. 4. Optimal cost for Fuzzy model |</p>
<table>
<thead>
<tr>
<th>Parameter (b)</th>
<th>% change</th>
<th>Value of the Parameter</th>
<th>Optimal cost for Fuzzy model</th>
</tr>
</thead>
<tbody>
<tr>
<td>.5</td>
<td>+25%</td>
<td>0.625</td>
<td>21.74064</td>
</tr>
<tr>
<td>.5</td>
<td>-25%</td>
<td>0.375</td>
<td>31.64027</td>
</tr>
<tr>
<td>.5</td>
<td>50%</td>
<td>0.75</td>
<td>18.56097</td>
</tr>
<tr>
<td>.5</td>
<td>-50%</td>
<td>0.25</td>
<td>40.96829</td>
</tr>
</tbody>
</table>
The deterministic model as well as the fuzzy model is highly sensitive to the demand parameters $a$, $b$ and production parameter $\beta$. In deterministic model as the value of $a$ and $b$ increases the total variable cost decreases and vice versa. But when the value of $\beta$ increases the total variable cost also increases. But in case of fuzzy model any increase or decrease in the value of $\beta$ makes the model infeasible. And as the value of $\beta$ increases the total variable cost decreases and vice-versa.

7. Conclusion.

In the present paper an EPQ model of time dependent deteriorating items has been studied and a methodology has been developed to determine the total average cost in fuzzy sense and to minimize the same. The basic assumption of the model is production is demand dependent which is exponential in nature. In reality, in different systems, there are some parameters which are imprecise in nature. The present paper proposes a solution procedure to develop an EPQ inventory model with variable production rate and fuzzy demand. In most of the real life problem, the demand in the market of the product which is being launched is uncertain. This justifies the introduction of fuzzy demand. To make the model more realistic demand has been fuzzified. This fuzzy parameters are then represented in terms of interval numbers. The original inventory model with interval coefficients is transformed into an equivalent multiobjective deterministic model. The multiobjective model is then solved by Global Criteria Method with the help of GRG (Generalized Reduced Gradient) technique. In future this model can be extended by taking deterioration parameter as fuzzy.

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References


